MARK SCHEME for the October/November 2012 series

4037 ADDITIONAL MATHEMATICS

4037/13 Paper 1, maximum raw mark 80

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes should be read in conjunction with the question paper and the Principal Examiner Report for Teachers.

Cambridge will not enter into discussions about these mark schemes.

Cambridge is publishing the mark schemes for the October/November 2012 series for most IGCSE, GCE Advanced Level and Advanced Subsidiary Level components and some Ordinary Level components.



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Mark Scheme Notes

Marks are of the following three types:

- M Method mark, awarded for a valid method applied to the problem. Method marks are not lost for numerical errors, algebraic slips or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using some method or just to quote a formula; the formula or idea must be applied to the specific problem in hand, e.g. by substituting the relevant quantities into the formula. Correct application of a formula without the formula being quoted obviously earns the M mark and in some cases an M mark can be implied from a correct answer.
- A Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated method mark is earned (or implied).
- B Accuracy mark for a correct result or statement independent of method marks.
- When a part of a question has two or more "method" steps, the M marks are generally independent unless the scheme specifically says otherwise; and similarly when there are several B marks allocated. The notation DM or DB (or dep*) is used to indicate that a particular M or B mark is dependent on an earlier M or B (asterisked) mark in the scheme. When two or more steps are run together by the candidate, the earlier marks are implied and full credit is given.
- The symbol √ implies that the A or B mark indicated is allowed for work correctly following on from previously incorrect results. Otherwise, A or B marks are given for correct work only. A and B marks are not given for fortuitously "correct" answers or results obtained from incorrect working.
- Note: B2 or A2 means that the candidate can earn 2 or 0.
 B2, 1, 0 means that the candidate can earn anything from 0 to 2.

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The following abbreviations may be used in a mark scheme or used on the scripts:

- AG Answer Given on the question paper (so extra checking is needed to ensure that the detailed working leading to the result is valid)
- BOD Benefit of Doubt (allowed when the validity of a solution may not be absolutely clear)
- CAO Correct Answer Only (emphasising that no "follow through" from a previous error is allowed)
- ISW Ignore Subsequent Working
- MR Misread
- PA Premature Approximation (resulting in basically correct work that is insufficiently accurate)
- SOS See Other Solution (the candidate makes a better attempt at the same question)

Penalties

- MR –1 A penalty of MR –1 is deducted from A or B marks when the data of a question or part question are genuinely misread and the object and difficulty of the question remain unaltered. In this case all A and B marks then become "follow through √" marks. MR is not applied when the candidate misreads his own figures – this is regarded as an error in accuracy.
- OW –1,2 This is deducted from A or B marks when essential working is omitted.
- PA –1 This is deducted from A or B marks in the case of premature approximation.
- S –1 Occasionally used for persistent slackness usually discussed at a meeting.
- EX –1 Applied to A or B marks when extra solutions are offered to a particular equation. Again, this is usually discussed at the meeting.

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1	$F \cap B =$	$P \rightarrow F, F \subseteq B \text{ and } B \supseteq F,$ $F \text{ or } F \cup B = B$ $\emptyset, S \cap F = \{\} \text{ or } F = 0$	B1 B1 B1 B1	[2] [1]			
2	(i) 3 or $\frac{3}{1}$)-0	B1	[1]			
	(ii) $\frac{dy}{dx} = \frac{3\sin t}{4\cos^2 t}$ $= \frac{3\sin\frac{\pi}{6}}{3}$	$\left(=\frac{3\sin t}{3}\right)$	M1 DM1		M1 correct	substitution in $\frac{d}{d}$	$\frac{y}{x} = \frac{dy}{dt} \times \frac{dt}{dx}$ o.e.
	= 0.5		A1	[3]	DM1 for u	se of their '3' and	substitution of $\frac{\pi}{6}$.
3	(i) ${}^{15}C_7 = 6435$ (ii) ${}^{6}C_2 \times {}^{9}C_5 = 1$	890	B1 M1,A	[1] 1 [2]	M1 for a co	orrect method	
	(iii) No women: 6435 – 36 = 6399	${}^{9}C_{7} = 36$	B1 M1 A1	[3]	B1 for 9C_7 M1 for a co	n = 36 omplete, correct r	nethod
4	(i)		B1 B1, B	1 [3]		in 2 <i>x</i> pe of <u>curve</u>	and finishing at 1
	(ii) $\left(\frac{\pi}{4}, 4\right)$ and	$\left(\frac{3\pi}{4}, -2\right)$	B1, B	1 [2]	B1 for each correct	h or B1 for both x	coordinates
	(iii) 3		B1ft	[1]	Ft from the	eir (i) or correct	

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5	(i) α β.	80 β 320 or 320 80	B1	B1 for correct triangle Could be implied by subsequent working		
	$\frac{320}{\sin 120^\circ}$	80	M1		mplete method (sin e) to find α or β	e rule and/or
	$\alpha = 12.5^{\circ}$	(or $\beta = 47.5^{\circ}$)	A1	A1 for α ((or β)	
	Bearing =	= 042.5° or 043°	A1 [4]	A1 for be	aring	
	(ii) $\frac{v_r}{\sin 47.5^\circ}$	$v_r = \frac{320}{\sin 120^\circ}, v_r = 272.4$	M1		the of complete meth sine rule) to find v_r	od (sine rule
	or $\frac{x}{\sin 120}$	$rac{1}{0^{\circ}} = rac{450}{\sin 47.5^{\circ}}$	A1	or x For either $v = 272$ or $x = 529$ DM1 for $\frac{450}{\text{their velocity}}$		
	Time = $-\frac{1}{2}$	$\frac{450}{272.4}$ or $\frac{528.6}{320}$	DM1			
	= 1.65		A1 [4]	or their $\frac{1}{3}$	$\frac{x}{20}$	
6	$(n+x)^6 = n^6$	$+6p^5x+15p^4x^2+20p^3x^3$				
	(i) $15p^4 = \frac{3}{2}$ p = 2		B1, B1 M1 A1 [4]		p^4 , B1 for $20p^3$ prrect attempt to equ	late
	(ii) need p^6	$(1)+6p^{5}(-2)+15p^{4}(1)$	B1		th $p^6, 6p^5$ (allow i	2
	= - 80		M1 A1 [3]		tempt using 3 terms g and adding at lease to $f x$	

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7 (i) $\frac{dx}{dt} = \frac{\left(t^2 + \frac{dx}{dt}\right)^2}{\left(\frac{dx}{dt}\right)^2}$ When $\frac{dx}{dt}$	$\frac{(-1)-t(2t)}{t^2+1}^2$ = 0, t=1 so $x=\frac{1}{2}$	M1 A1 DM1 A1		product A1 all cor		-
	$\frac{-2t}{\left(t^{2}+1\right)^{4}} = -0.5$	M1 A1 A1	[4]	M1 for att	2 tempt to differentia o find acceleration at unsimplified	ate a quotient or
p = -26 $a = 3, b$	(+20 + 2p + 8 = 0) = 11, c = -4 (3x - 1)(x + 4)	M1 A1 B3 M1 A1	[5]	comparing division B1 for eac	e of 2 and equating g coefficients or al ch of a, b and c tempt to obtain 3 f	
	$r^{2} + 10^{2} - 2(20)(10)\cos\frac{5\pi}{6}$ $r = \frac{10\pi}{6} + \frac{20\pi}{6} + 2(29.1)$	M1 B1 DM1 A1	[4]	square roo B1 for eit	ther arc length correct plan before c lengths and <i>AD</i>	-
(ii) Area = $\frac{1}{2}10^2 \left(\frac{\pi}{6}\right) + \frac{1}{2}20^2 \left(\frac{\pi}{6}\right) = 231$	$\left(\frac{\pi}{6}\right) + 2\left(\frac{1}{2}(10)(20)\sin\frac{5\pi}{6}\right)$	M1 B1 DM1 A1	[4]	complete B1 for ½ DM1 for	ea of triangle using correct method $10^2(\pi/6)$ or $\frac{1}{2} 20^2(\pi/6)$ correct plan before ctor and triangle a	τ/6) evaluation using

	Pa	ge 7	Mark Sche			Syllabus	Paper			
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10	(i)	$\sec x (\sec \cos x) = 0.$		M1 M1 A1, A1 [4]	M1 for so	M1 for use of correct identity M1 for solution of quadratic in sec of A1 for one correct solution				
		$\sin^2 x - 2$	he: $\frac{2}{\cos x} + 1 = 0$ $\cos x + \cos^2 x = 0$, $5, x = 60^\circ, 300^\circ$		for use of	aling with tan and s correct identity lution to obtain cos	-			
	(ii)		$=\frac{1}{5}, \tan 3y = (\pm)\frac{1}{\sqrt{5}}$ $y = (\pm)\frac{1}{\sqrt{6}}, \cos 3y = (\pm)\frac{\sqrt{5}}{\sqrt{6}}$	M1		M1 for correctly obtaining in terms of 1 trig ratio and square rooting				
		3y = 0.42	$\sqrt{6}$ $\sqrt{6}$, 2.72, etc. , 0.907, 1.19, 1.95	M1 A1, A1 [4]		ealing with '3' correst A1 for others	ectly			
	(iii)	$\sin\left(z+\frac{\pi}{4}\right)$	$\left(-\right) = \frac{2}{5}$	M1	M1 for de	aling with '2' and c	cosec correctly			
		$z + \frac{\pi}{4} = 0.4$ $z = 1.94,$	4115, 2.730, 6.695	DM1 A1,A1	DM1 for o	dealing with $\frac{\pi}{4}$ co	rrectly			
		2 1.94,	5.71	[4]						
11	EIT	HER								
	(i)	$\frac{\mathrm{d}y}{\mathrm{d}x} = 5e^x -$		B1	B1 For co	prrect derivative				
			$=\ln\frac{3}{5}, \ \frac{\mathrm{d}y}{\mathrm{d}x} = -2$	B1	B1 for gra	ad = -2 from correc	t working			
		When $x =$	$\sin \frac{3}{5}, y = 8$	B1	B1 for $y =$	1 for $y = 8$				
		Tangent:	$y-8=-2\left(x-\ln\frac{3}{5}\right)$	M1	Equation their 8	of a tangent using t	heir gradient and			
		When <i>y</i> =	=0, $x=4+\ln\frac{3}{5}$ (3.49)	A1 [5]						
	(ii)	$\int_0^a 5e^x + 3$	$Be^{-x} dx = 12$	B1	B1 for con	rrect integration				
		$5e^x - 3e^{-1}$								
		$5e^{a} - 3e^{-a}$	a - 2 = 12	M1	M1 for correct use of limits					
		$5e^{2a} - 14e^{2a}$	$e^{a} - 3 = 0$	A1 [3]	Answer g manipulat	iven so need to see tion	some			
	/***	(
	(iii)		$(e^{a} - 3) = 0$ 1.1 or 1.10	M1 M1 A1		cognising and deali rrect method of sol				
				[3]						

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11	OR (i) $\frac{dy}{dx} = \frac{(1+x)^{2}}{(1+e^{2x})^{2}}$	$\frac{-e^{2x}}{(1+e^{2x})^2} \frac{6e^{2x}-3e^{2x}(2e^{2x})}{(1+e^{2x})^2}$	M1 A2,1,0)	M1 for at product -1 each e	tempt to differentiat	e a quotient or
	$\begin{pmatrix} 1 + e^{2x} \\ \therefore A = 6 \end{pmatrix}$	2	A1	[4]	For 6 obta	ained from correct v	vorking.
	(ii) When x	$=0, y=\frac{3}{2}$	B1		B1 for <i>y</i> =	$=\frac{3}{2}$	
	$\frac{\mathrm{d}y}{\mathrm{d}x} = \frac{3}{2}$		B1ft		B1 for gra	$\operatorname{ad} = \frac{A}{4}$	
	$\therefore y - \frac{3}{2}$	$=\frac{3}{2}x$	B1ft	[3]	Ft their y_0	and $\frac{A}{4}$	
	(iii)	x (2x)					
	$\int \frac{e^{2}}{(1+a)}$	$\frac{dx}{(2x)^2} dx = \frac{1}{2} \left(\frac{e^{2x}}{(1+e^{2x})} \right) (+c)$	M1			tempt at 'reverse di	
	() ((),)	A1ft		Ft on thei	rA , i.e. $\frac{3}{A}$ for a co	orrect statement
	$\frac{1}{2}\left[\begin{array}{c} e \\ \overline{1+} \end{array}\right]$	$\left[\frac{2x}{e^{2x}}\right]_{0}^{\ln 3} = \frac{1}{2} \left(\frac{9}{10} - \frac{1}{2}\right)$	M1		M1 for co	prrect use of limits	
	= 0.2		A1ft	[4]	Ft $\frac{A}{30}$		